Package: spBPS (via r-universe)

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Title Bayesian Predictive Stacking for Scalable Geospatial Transfer Learning

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Description Provides functions for Bayesian Predictive Stacking within the Bayesian transfer learning framework for geospatial artificial systems, as introduced in ``Bayesian Transfer Learning for Artificially Intelligent Geospatial Systems: A Predictive Stacking Approach" (Presicce and Banerjee, 2024) <doi:10.48550/arXiv.2410.09504>. This methodology enables efficient Bayesian geostatistical modeling, utilizing predictive stacking to improve inference across spatial datasets. The core functions leverage 'C++' for high-performance computation, making the framework well-suited for large-scale spatial data analysis in parallel and distributed computing environments. Designed for scalability, it allows seamless application in computationally demanding scenarios.

Depends R (>= 1.8.0)

Imports Rcpp, CVXR, mniw

LinkingTo Rcpp, RcppArmadillo

Suggests knitr, rmarkdown, mvnfast, foreach, parallel, doParallel, tictoc, MBA, RColorBrewer, classInt, sp, fields, testthat (>= 3.0.0)

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VignetteBuilder knitr

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Contents

`arma_dist` *Compute the Euclidean distance matrix*

Description

Compute the Euclidean distance matrix

Usage

```
arma_dist(X)
```

Arguments

`X`	matrix (tipically of N coordindates on $\mathbb{R}^2$)

Value

matrix distance matrix of the elements of X

Examples

```
## Compute the Distance matrix of dimension (n x n)
n <- 100
p <- 2
X <- matrix(runif(n*p), nrow = n, ncol = p)
distance.matrix <- arma_dist(X)
```

`bayesMvLMconjugate` *Gibbs sampler for Conjugate Bayesian Multivariate Linear Models*

Description

Gibbs sampler for Conjugate Bayesian Multivariate Linear Models

Usage

```
bayesMvLMconjugate(Y, X, mu_B, V_B, nu, Psi, n_iter = 1000, burn_in = 500)
```

Arguments

Y	matrix $n \times q$ of response variables
X	matrix $n \times p$ of predictors
mu_B	matrix $p \times q$ prior mean for β
V_B	matrix $p \times p$ prior row covariance for β
nu	double prior parameter for Σ
Psi	matrix prior parameter for Σ
n_iter	integer iteration number for Gibbs sampler
burn_in	integer number of burn-in iteration

Value

B_samples array of posterior sample for β

Sigma_samples array of posterior samples for Σ

Examples

```
## Generate data
n <- 100
p <- 3
q <- 2
Y <- matrix(rnorm(n*q), nrow = n, ncol = q)
X <- matrix(rnorm(n*p), nrow = n, ncol = p)

## Prior parameters
mu_B <- matrix(0, p, q)
V_B <- diag(10, p)
nu <- 3
Psi <- diag(q)

## Samples from posteriors
n_iter <- 1000
burn_in <- 500
set.seed(1234)
samples <- spBPS::bayesMvLMconjugate(Y, X, mu_B, V_B, nu, Psi, n_iter, burn_in)
```

BPS_combine *Combine subset models wiht BPS*

Description

Combine subset models wiht BPS

Usage

```
BPS_combine(fit_list, K, rp)
```

Arguments

`fit_list`	list K fitted model outputs composed by two elements each: first named epd, second named W
`K`	integer number of folds
`rp`	double percentage of observations to take into account for optimization (`default=1`)

Value

matrix posterior predictive density evaluations (each columns represent a different model)

Examples

```
## Generate subsets of data
n <- 100
p <- 3
X <- matrix(rnorm(n*p), nrow = n, ncol = p)
Y <- matrix(rnorm(n), nrow = n, ncol = 1)
crd <- matrix(runif(n*2), nrow = n, ncol = 2)
data_part <- subset_data(data = list(Y = Y, X = X, crd = crd), K = 10)

## Select competitive set of values for hyperparameters
delta_seq <- c(0.1, 0.2, 0.3)
phi_seq <- c(3, 4, 5)

## Perform Bayesian Predictive Stacking within subsets
fit_list <- vector(length = 10, mode = "list")
for (i in 1:10) {
    Yi <- data_part$Y_list[[i]]
    Xi <- data_part$X_list[[i]]
    crd_i <- data_part$crd_list[[i]]
    p <- ncol(Xi)
    bps <- spBPS::BPS_weights(data = list(Y = Yi, X = Xi),
                              priors = list(mu_b = matrix(rep(0, p)),
                                            V_b = diag(10, p),
                                            a = 2,
                                            b = 2), coords = crd_i,
                                            hyperpar = list(delta = delta_seq,
                                                            phi = phi_seq),
                                            K = 5)
     w_hat <- bps$W
     epd <- bps$epd
     fit_list[[i]] <- list(epd, w_hat) }

## Combination weights between partitions using Bayesian Predictive Stacking
comb_bps <- BPS_combine(fit_list = fit_list, K = 10, rp = 1)
```

BPS_post *Perform the BPS sampling from posterior and posterior predictive given a set of stacking weights*

Description

Perform the BPS sampling from posterior and posterior predictive given a set of stacking weights

Usage

```
BPS_post(data, X_u, priors, coords, crd_u, hyperpar, W, R)
```

Arguments

data	list two elements: first named Y, second named X
X_u	matrix unobserved instances covariate matrix
priors	list priors: named μ_b,V_b,a,b
coords	matrix sample coordinates for X and Y
crd_u	matrix unboserved instances coordinates
hyperpar	list two elemets: first named δ, second named ϕ
W	matrix set of stacking weights
R	integer number of desired samples

Value

list BPS posterior predictive samples

Examples

```
## Generate subsets of data
n <- 100
p <- 3
X <- matrix(rnorm(n*p), nrow = n, ncol = p)
Y <- matrix(rnorm(n), nrow = n, ncol = 1)
crd <- matrix(runif(n*2), nrow = n, ncol = 2)
data_part <- subset_data(data = list(Y = Y, X = X, crd = crd), K = 10)

## Select competetive set of values for hyperparameters
delta_seq <- c(0.1, 0.2, 0.3)
phi_seq <- c(3, 4, 5)
## Fit local models
fit_list <- vector(length = 10, mode = "list")
for (i in 1:10) {
  Yi <- data_part$Y_list[[i]]
  Xi <- data_part$X_list[[i]]
  crd_i <- data_part$crd_list[[i]]
  p <- ncol(Xi)
```

```
  bps <- spBPS::BPS_weights(data = list(Y = Yi, X = Xi),
                            priors = list(mu_b = matrix(rep(0, p)),
                                          V_b = diag(10, p),
                                          a = 2,
                                          b = 2), coords = crd_i,
                                          hyperpar = list(delta = delta_seq,
                                                          phi = phi_seq),
                                                          K = 5)
  w_hat <- bps$W
  epd <- bps$epd
  fit_list[[i]] <- list(epd, w_hat) }

## Model combination weights between partitions using Bayesian Predictive Stacking
comb_bps <- BPS_combine(fit_list = fit_list, K = 10, rp = 1)
Wbps <- comb_bps$W
W_list <- comb_bps$W_list

## Generate prediction points
m <- 100
X_new <- matrix(rnorm(m*p), nrow = m, ncol = p)
crd_new <- matrix(runif(m*2), nrow = m, ncol = 2)

## Perform posterior and posterior predictive sampling
R <- 250
subset_ind <- sample(1:10, R, TRUE, Wbps)
postsmp_and_pred <- vector(length = R, mode = "list")
for (r in 1:R) {
 ind_s <- subset_ind[r]
 Ys <- matrix(data_part$Y_list[[ind_s]])
 Xs <- data_part$X_list[[ind_s]]
 crds <- data_part$crd_list[[ind_s]]
 Ws <- W_list[[ind_s]]
 result <- spBPS::BPS_post(data = list(Y = Ys, X = Xs), coords = crds,
                           X_u = X_new, crd_u = crd_new,
                           priors = list(mu_b = matrix(rep(0, p)),
                                         V_b = diag(10, p),
                                         a = 2,
                                         b = 2),
                                         hyperpar = list(delta = delta_seq,
                                                         phi = phi_seq),
                                                         W = Ws, R = 1)
 postsmp_and_pred[[r]] <- result}
```

BPS_postdraws *Compute the BPS posterior samples given a set of stacking weights*

Description

Compute the BPS posterior samples given a set of stacking weights

Usage

```
BPS_postdraws(data, priors, coords, hyperpar, W, R)
```

Arguments

data	list two elements: first named Y, second named X
priors	list priors: named μ_b,V_b,a,b
coords	matrix sample coordinates for X and Y
hyperpar	list two elemets: first named δ, second named ϕ
W	matrix set of stacking weights
R	integer number of desired samples

Value

matrix BPS posterior samples

BPS_postdraws_MvT *Compute the BPS posterior samples given a set of stacking weights*

Description

Compute the BPS posterior samples given a set of stacking weights

Usage

```
BPS_postdraws_MvT(data, priors, coords, hyperpar, W, R, par)
```

Arguments

data	list two elements: first named Y, second named X
priors	list priors: named μ_B,V_r,Ψ,ν
coords	matrix sample coordinates for X and Y
hyperpar	list two elemets: first named α, second named ϕ
W	matrix set of stacking weights
R	integer number of desired samples
par	if TRUE only β and Σ are sampled (ω is omitted)

Value

matrix BPS posterior samples

`BPS_post_MvT` *Perform the BPS sampling from posterior and posterior predictive given a set of stacking weights*

Description

Perform the BPS sampling from posterior and posterior predictive given a set of stacking weights

Usage

```
BPS_post_MvT(data, X_u, priors, coords, crd_u, hyperpar, W, R)
```

Arguments

`data`	list two elements: first named Y, second named X
`X_u`	matrix unobserved instances covariate matrix
`priors`	list priors: named μ_B,V_r,Ψ,ν
`coords`	matrix sample coordinates for X and Y
`crd_u`	matrix unboserved instances coordinates
`hyperpar`	list two elemets: first named α, second named ϕ
`W`	matrix set of stacking weights
`R`	integer number of desired samples

Value

list BPS posterior predictive samples

Examples

```
## Generate subsets of data
n <- 100
p <- 3
q <- 2
X <- matrix(rnorm(n*p), nrow = n, ncol = p)
Y <- matrix(rnorm(n*q), nrow = n, ncol = q)
crd <- matrix(runif(n*2), nrow = n, ncol = 2)
data_part <- subset_data(data = list(Y = Y, X = X, crd = crd), K = 10)

## Select competitive set of values for hyperparameters
alfa_seq <- c(0.7, 0.8, 0.9)
phi_seq <- c(3, 4, 5)

## Fit local models
fit_list <- vector(length = 10, mode = "list")
for (i in 1:10) {
    Yi <- data_part$Y_list[[i]]
    Xi <- data_part$X_list[[i]]
```

```
    crd_i <- data_part$crd_list[[i]]
    bps <- spBPS::BPS_weights_MvT(data = list(Y = Yi, X = Xi),
                            priors = list(mu_B = matrix(0, nrow = p, ncol = q),
                                          V_r = diag(10, p),
                                          Psi = diag(1, q),
                                          nu = 3), coords = crd_i,
                                          hyperpar = list(alpha = alfa_seq,
                                                          phi = phi_seq),
                                          K = 5)
     w_hat <- bps$W
     epd <- bps$epd
     fit_list[[i]] <- list(epd, w_hat) }

## Model combination weights between partitions using Bayesian Predictive Stacking
comb_bps <- BPS_combine(fit_list = fit_list, K = 10, rp = 1)
Wbps <- comb_bps$W
W_list <- comb_bps$W_list

## Generate prediction points
m <- 100
X_new <- matrix(rnorm(m*p), nrow = m, ncol = p)
crd_new <- matrix(runif(m*2), nrow = m, ncol = 2)

## Perform posterior and posterior predictive sampling
R <- 250
subset_ind <- sample(1:10, R, TRUE, Wbps)
postsmp_and_pred <- vector(length = R, mode = "list")
for (r in 1:R) {
  ind_s <- subset_ind[r]
  Ys <- data_part$Y_list[[ind_s]]
  Xs <- data_part$X_list[[ind_s]]
  crds <- data_part$crd_list[[ind_s]]
  Ws <- W_list[[ind_s]]
  result <- spBPS::BPS_post_MvT(data = list(Y = Ys, X = Xs), coords = crds,
                                X_u = X_new, crd_u = crd_new,
                                priors = list(mu_B = matrix(0, nrow = p, ncol = q),
                                              V_r = diag(10, p),
                                              Psi = diag(1, q),
                                              nu = 3),
                                              hyperpar = list(alpha = alfa_seq,
                                                              phi = phi_seq),
                                              W = Ws, R = 1)

  postsmp_and_pred[[r]] <- result}
```

BPS_pred *Compute the BPS spatial prediction given a set of stacking weights*

Description

Compute the BPS spatial prediction given a set of stacking weights

Usage

```
BPS_pred(data, X_u, priors, coords, crd_u, hyperpar, W, R)
```

Arguments

data	list two elements: first named Y, second named X
X_u	matrix unobserved instances covariate matrix
priors	list priors: named μ_b,V_b,a,b
coords	matrix sample coordinates for X and Y
crd_u	matrix unboserved instances coordinates
hyperpar	list two elemets: first named δ, second named ϕ
W	matrix set of stacking weights
R	integer number of desired samples

Value

list BPS posterior predictive samples

Examples

```
## Generate subsets of data
n <- 100
p <- 3
X <- matrix(rnorm(n*p), nrow = n, ncol = p)
Y <- matrix(rnorm(n), nrow = n, ncol = 1)
crd <- matrix(runif(n*2), nrow = n, ncol = 2)
data_part <- subset_data(data = list(Y = Y, X = X, crd = crd), K = 10)

## Select competetive set of values for hyperparameters
delta_seq <- c(0.1, 0.2, 0.3)
phi_seq <- c(3, 4, 5)

## Fit local models
fit_list <- vector(length = 10, mode = "list")
for (i in 1:10) {
    Yi <- data_part$Y_list[[i]]
    Xi <- data_part$X_list[[i]]
    crd_i <- data_part$crd_list[[i]]
    p <- ncol(Xi)
    bps <- spBPS::BPS_weights(data = list(Y = Yi, X = Xi),
                              priors = list(mu_b = matrix(rep(0, p)),
                                            V_b = diag(10, p),
                                            a = 2,
                                            b = 2), coords = crd_i,
                                            hyperpar = list(delta = delta_seq,
```

```
                                                          phi = phi_seq),
                                              K = 5)
    w_hat <- bps$W
    epd <- bps$epd
    fit_list[[i]] <- list(epd, w_hat) }

## Model combination weights between partitions using Bayesian Predictive Stacking
comb_bps <- BPS_combine(fit_list = fit_list, K = 10, rp = 1)
Wbps <- comb_bps$W
W_list <- comb_bps$W_list

## Generate prediction points
m <- 50
X_new <- matrix(rnorm(m*p), nrow = m, ncol = p)
crd_new <- matrix(runif(m*2), nrow = m, ncol = 2)

## Perform posterior predictive sampling
R <- 250
subset_ind <- sample(1:10, R, TRUE, Wbps)
predictions <- vector(length = R, mode = "list")
for (r in 1:R) {
  ind_s <- subset_ind[r]
  Ys <- matrix(data_part$Y_list[[ind_s]])
  Xs <- data_part$X_list[[ind_s]]
  crds <- data_part$crd_list[[ind_s]]
  Ws <- W_list[[ind_s]]
  result <- spBPS::BPS_pred(data = list(Y = Ys, X = Xs), coords = crds,
                            X_u = X_new, crd_u = crd_new,
                            priors = list(mu_b = matrix(rep(0, p)),
                                          V_b = diag(10, p),
                                          a = 2,
                                          b = 2),
                                          hyperpar = list(delta = delta_seq,
                                                          phi = phi_seq),
                                          W = Ws, R = 1)

  predictions[[r]] <- result}
```

BPS_pred_MvT *Compute the BPS spatial prediction given a set of stacking weights*

Description

Compute the BPS spatial prediction given a set of stacking weights

Usage

```
BPS_pred_MvT(data, X_u, priors, coords, crd_u, hyperpar, W, R)
```

Arguments

data	list two elements: first named Y, second named X
X_u	matrix unobserved instances covariate matrix
priors	list priors: named μ_B,V_r,Ψ,ν
coords	matrix sample coordinates for X and Y
crd_u	matrix unboserved instances coordinates
hyperpar	list two elemets: first named α, second named ϕ
W	matrix set of stacking weights
R	integer number of desired samples

Value

list BPS posterior predictive samples

Examples

```
## Generate subsets of data
n <- 100
p <- 3
q <- 2
X <- matrix(rnorm(n*p), nrow = n, ncol = p)
Y <- matrix(rnorm(n*q), nrow = n, ncol = q)
crd <- matrix(runif(n*2), nrow = n, ncol = 2)
data_part <- subset_data(data = list(Y = Y, X = X, crd = crd), K = 10)

## Select competitive set of values for hyperparameters
alfa_seq <- c(0.7, 0.8, 0.9)
phi_seq <- c(3, 4, 5)

## Fit local models
fit_list <- vector(length = 10, mode = "list")
for (i in 1:10) {
    Yi <- data_part$Y_list[[i]]
    Xi <- data_part$X_list[[i]]
    crd_i <- data_part$crd_list[[i]]
    bps <- spBPS::BPS_weights_MvT(data = list(Y = Yi, X = Xi),
                              priors = list(mu_B = matrix(0, nrow = p, ncol = q),
                                            V_r = diag(10, p),
                                            Psi = diag(1, q),
                                            nu = 3), coords = crd_i,
                                            hyperpar = list(alpha = alfa_seq,
                                                            phi = phi_seq),
                                            K = 5)
     w_hat <- bps$W
     epd <- bps$epd
     fit_list[[i]] <- list(epd, w_hat) }

## Model combination weights between partitions using Bayesian Predictive Stacking
comb_bps <- BPS_combine(fit_list = fit_list, K = 10, rp = 1)
```

```
Wbps <- comb_bps$W
W_list <- comb_bps$W_list

## Generate prediction points
m <- 100
X_new <- matrix(rnorm(m*p), nrow = m, ncol = p)
crd_new <- matrix(runif(m*2), nrow = m, ncol = 2)

## Perform posterior predictive sampling
R <- 250
subset_ind <- sample(1:10, R, TRUE, Wbps)
predictions <- vector(length = R, mode = "list")
for (r in 1:R) {
  ind_s <- subset_ind[r]
  Ys <- data_part$Y_list[[ind_s]]
  Xs <- data_part$X_list[[ind_s]]
  crds <- data_part$crd_list[[ind_s]]
  Ws <- W_list[[ind_s]]
  result <- spBPS::BPS_pred_MvT(data = list(Y = Ys, X = Xs), coords = crds,
                                X_u = X_new, crd_u = crd_new,
                                priors = list(mu_B = matrix(0, nrow = p, ncol = q),
                                              V_r = diag(10, p),
                                              Psi = diag(1, q),
                                              nu = 3),
                                              hyperpar = list(alpha = alfa_seq,
                                                              phi = phi_seq),
                                              W = Ws, R = 1)

  predictions[[r]] <- result}
```

BPS_PseudoBMA *Combine subset models wiht Pseudo-BMA*

Description

Combine subset models wiht Pseudo-BMA

Usage

```
BPS_PseudoBMA(fit_list)
```

Arguments

fit_list	list K fitted model outputs composed by two elements each: first named epd, second named W

Value

matrix posterior predictive density evaluations (each columns represent a different model)

Examples

```
## Generate subsets of data
n <- 100
p <- 3
X <- matrix(rnorm(n*p), nrow = n, ncol = p)
Y <- matrix(rnorm(n), nrow = n, ncol = 1)
crd <- matrix(runif(n*2), nrow = n, ncol = 2)
data_part <- subset_data(data = list(Y = Y, X = X, crd = crd), K = 10)

## Select competitive set of values for hyperparameters
delta_seq <- c(0.1, 0.2, 0.3)
phi_seq <- c(3, 4, 5)

## Perform Bayesian Predictive Stacking within subsets
fit_list <- vector(length = 10, mode = "list")
for (i in 1:10) {
    Yi <- data_part$Y_list[[i]]
    Xi <- data_part$X_list[[i]]
    crd_i <- data_part$crd_list[[i]]
    p <- ncol(Xi)
    bps <- spBPS::BPS_weights(data = list(Y = Yi, X = Xi),
                              priors = list(mu_b = matrix(rep(0, p)),
                                            V_b = diag(10, p),
                                            a = 2,
                                            b = 2), coords = crd_i,
                                            hyperpar = list(delta = delta_seq,
                                                            phi = phi_seq),
                                            K = 5)
     w_hat <- bps$W
     epd <- bps$epd
     fit_list[[i]] <- list(epd, w_hat) }

## Combination weights between partitions using Pseudo Bayesian Model Averaging
comb_bps <- BPS_PseudoBMA(fit_list = fit_list)
```

BPS_weights *Compute the BPS weights by convex optimization*

Description

Compute the BPS weights by convex optimization

Usage

```
BPS_weights(data, priors, coords, hyperpar, K)
```

Arguments

data	list two elements: first named Y, second named X
priors	list priors: named μ_b,V_b,a,b
coords	matrix sample coordinates for X and Y
hyperpar	list two elemets: first named δ, second named ϕ
K	integer number of folds

Value

matrix posterior predictive density evaluations (each columns represent a different model)

Examples

```
## Generate subsets of data
n <- 100
p <- 3
X <- matrix(rnorm(n*p), nrow = n, ncol = p)
Y <- matrix(rnorm(n), nrow = n)
crd <- matrix(runif(n*2), nrow = n, ncol = 2)

## Select competitive set of values for hyperparameters
delta_seq <- c(0.1, 0.2, 0.3)
phi_seq <- c(3, 4, 5)

## Perform Bayesian Predictive Stacking within subsets
bps <- spBPS::BPS_weights(data = list(Y = Y, X = X),
                          priors = list(mu_b = matrix(rep(0, p)),
                                        V_b = diag(10, p),
                                        a = 2,
                                        b = 2), coords = crd,
                                        hyperpar = list(delta = delta_seq,
                                                        phi = phi_seq),
                                        K = 5)
```

BPS_weights_MvT *Compute the BPS weights by convex optimization*

Description

Compute the BPS weights by convex optimization

Usage

```
BPS_weights_MvT(data, priors, coords, hyperpar, K)
```

Arguments

data	list two elements: first named Y, second named X
priors	list priors: named μ_B,V_r,Ψ,ν
coords	matrix sample coordinates for X and Y
hyperpar	list two elemets: first named α, second named ϕ
K	integer number of folds

Value

matrix posterior predictive density evaluations (each columns represent a different model)

Examples

```
## Generate subsets of data
n <- 100
p <- 3
q <- 2
X <- matrix(rnorm(n*p), nrow = n, ncol = p)
Y <- matrix(rnorm(n*q), nrow = n, ncol = q)
crd <- matrix(runif(n*2), nrow = n, ncol = 2)

## Select competitive set of values for hyperparameters
alfa_seq <- c(0.7, 0.8, 0.9)
phi_seq <- c(3, 4, 5)

## Perform Bayesian Predictive Stacking within subsets
bps <- spBPS::BPS_weights_MvT(data = list(Y = Y, X = X),
                              priors = list(mu_B = matrix(0, nrow = p, ncol = q),
                                            V_r = diag(10, p),
                                            Psi = diag(1, q),
                                            nu = 3), coords = crd,
                                            hyperpar = list(alpha = alfa_seq,
                                                            phi = phi_seq),
                                            K = 5)
```

---

conv_opt *Solver for Bayesian Predictive Stacking of Predictive densities convex optimization problem*

Description

Solver for Bayesian Predictive Stacking of Predictive densities convex optimization problem

Usage

```
conv_opt(scores)
```

Arguments

scores	matrix $N \times K$ of expected predictive density evaluations for the K models considered

Value

W matrix of Bayesian Predictive Stacking weights for the K models considered

Examples

```
## Generate (randomly) K predictive scores for n observations
n <- 50
K <- 5
scores <- matrix(runif(n*K), nrow = n, ncol = K)

## Find Bayesian Predictive Stacking weights
opt_weights <- conv_opt(scores)
```

CVXR_opt *Compute the BPS weights by convex optimization*

Description

Compute the BPS weights by convex optimization

Usage

```
CVXR_opt(scores)
```

Arguments

scores	matrix $N \times K$ of expected predictive density evaluations for the K models considered

Value

conv_opt function to perform convex optimiazion with CVXR R package

dens_kcv *Compute the KCV of the density evaluations for fixed values of the hyperparameters*

Description

Compute the KCV of the density evaluations for fixed values of the hyperparameters

Usage

```
dens_kcv(data, priors, coords, hyperpar, K)
```

Arguments

data	list two elements: first named Y, second named X
priors	list priors: named μ_b,V_b,a,b
coords	matrix sample coordinates for X and Y
hyperpar	list two elemets: first named δ, second named ϕ
K	integer number of folds

Value

vector posterior predictive density evaluations

dens_kcv_MvT *Compute the KCV of the density evaluations for fixed values of the hyperparameters*

Description

Compute the KCV of the density evaluations for fixed values of the hyperparameters

Usage

```
dens_kcv_MvT(data, priors, coords, hyperpar, K)
```

Arguments

data	list two elements: first named Y, second named X
priors	list priors: named μ_B,V_r,Ψ,ν
coords	matrix sample coordinates for X and Y
hyperpar	list two elemets: first named α, second named ϕ
K	integer number of folds

Value

vector posterior predictive density evaluations

`dens_loocv` *Compute the LOOCV of the density evaluations for fixed values of the hyperparameters*

Description

Compute the LOOCV of the density evaluations for fixed values of the hyperparameters

Usage

```
dens_loocv(data, priors, coords, hyperpar)
```

Arguments

`data`	list two elements: first named Y, second named X
`priors`	list priors: named μ_b,V_b,a,b
`coords`	matrix sample coordinates for X and Y
`hyperpar`	list two elemets: first named δ, second named ϕ

Value

vector posterior predictive density evaluations

`dens_loocv_MvT` *Compute the LOOCV of the density evaluations for fixed values of the hyperparameters*

Description

Compute the LOOCV of the density evaluations for fixed values of the hyperparameters

Usage

```
dens_loocv_MvT(data, priors, coords, hyperpar)
```

Arguments

`data`	list two elements: first named Y, second named X
`priors`	list priors: named μ_B,V_r,Ψ,ν
`coords`	matrix sample coordinates for X and Y
`hyperpar`	list two elemets: first named α, second named ϕ

Value

vector posterior predictive density evaluations

`d_pred_cpp` *Evaluate the density of a set of unobserved response with respect to the conditional posterior predictive*

Description

Evaluate the density of a set of unobserved response with respect to the conditional posterior predictive

Usage

```
d_pred_cpp(data, X_u, Y_u, d_u, d_us, hyperpar, poster)
```

Arguments

`data`	list two elements: first named Y, second named X
`X_u`	matrix unobserved instances covariate matrix
`Y_u`	matrix unobserved instances response matrix
`d_u`	matrix unobserved instances distance matrix
`d_us`	matrix cross-distance between unobserved and observed instances matrix
`hyperpar`	list two elemets: first named δ, second named ϕ
`poster`	list output from `fit_cpp` function

Value

vector posterior predictive density evaluations

`d_pred_cpp_MvT` *Evaluate the density of a set of unobserved response with respect to the conditional posterior predictive*

Description

Evaluate the density of a set of unobserved response with respect to the conditional posterior predictive

Usage

```
d_pred_cpp_MvT(data, X_u, Y_u, d_u, d_us, hyperpar, poster)
```

Arguments

data	list two elements: first named Y, second named X
X_u	matrix unobserved instances covariate matrix
Y_u	matrix unobserved instances response matrix
d_u	matrix unobserved instances distance matrix
d_us	matrix cross-distance between unobserved and observed instances matrix
hyperpar	list two elemets: first named α, second named ϕ
poster	list output from fit_cpp function

Value

double posterior predictive density evaluation

---

expand_grid_cpp *Build a grid from two vector (i.e. equivalent to* expand.grid() *in* R*)*

Description

Build a grid from two vector (i.e. equivalent to expand.grid() in R)

Usage

```
expand_grid_cpp(x, y)
```

Arguments

x	vector first vector of numeric elements
y	vector second vector of numeric elements

Value

matrix expanded grid of combinations

Examples

```
## Create a matrix from all combination of vectors
x <- seq(0, 10, length.out = 100)
y <- seq(-1, 1, length.out = 20)
grid <- expand_grid_cpp(x = x, y = y)
```

`fit_cpp` *Compute the parameters for the posteriors distribution of β and Σ (i.e. updated parameters)*

Description

Compute the parameters for the posteriors distribution of β and Σ (i.e. updated parameters)

Usage

```
fit_cpp(data, priors, coords, hyperpar)
```

Arguments

`data`	list two elements: first named Y, second named X
`priors`	list priors: named μ_b,V_b,a,b
`coords`	matrix sample coordinates for X and Y
`hyperpar`	list two elemets: first named δ, second named ϕ

Value

list posterior update parameters

`fit_cpp_MvT` *Compute the parameters for the posteriors distribution of β and Σ (i.e. updated parameters)*

Description

Compute the parameters for the posteriors distribution of β and Σ (i.e. updated parameters)

Usage

```
fit_cpp_MvT(data, priors, coords, hyperpar)
```

Arguments

`data`	list two elements: first named Y, second named X
`priors`	list priors: named μ_B,V_r,Ψ,ν
`coords`	matrix sample coordinates for X and Y
`hyperpar`	list two elemets: first named α, second named ϕ

Value

list posterior update parameters

forceSymmetry_cpp *Function to subset data for meta-analysis*

Description

Function to subset data for meta-analysis

Usage

```
forceSymmetry_cpp(mat)
```

Arguments

mat	matrix not-symmetric matrix

Value

matrix symmetric matrix (lower triangular of `mat` is used)

Examples

```
## Force matrix to be symmetric (avoiding numerical problems)
n <- 4
X <- matrix(runif(n*n), nrow = n, ncol = n)
X <- forceSymmetry_cpp(mat = X)
```

models_dens *Return the CV predictive density evaluations for all the model combinations*

Description

Return the CV predictive density evaluations for all the model combinations

Usage

```
models_dens(data, priors, coords, hyperpar, useKCV, K)
```

Arguments

data	list two elements: first named Y, second named X
priors	list priors: named μ_b,V_b,a,b
coords	matrix sample coordinates for X and Y
hyperpar	list two elemets: first named δ, second named ϕ
useKCV	if `TRUE` K-fold cross validation is used instead of LOOCV (no `default`)
K	integer number of folds

Value

matrix posterior predictive density evaluations (each columns represent a different model)

`models_dens_MvT` *Return the CV predictive density evaluations for all the model combinations*

Description

Return the CV predictive density evaluations for all the model combinations

Usage

```
models_dens_MvT(data, priors, coords, hyperpar, useKCV, K)
```

Arguments

`data`	list two elements: first named Y, second named X
`priors`	list priors: named μ_B,V_r,Ψ,ν
`coords`	matrix sample coordinates for X and Y
`hyperpar`	list two elemets: first named α, second named ϕ
`useKCV`	if `TRUE` K-fold cross validation is used instead of LOOCV (no `default`)
`K`	integer number of folds

Value

matrix posterior predictive density evaluations (each columns represent a different model)

`post_draws` *Sample R draws from the posterior distributions*

Description

Sample R draws from the posterior distributions

Usage

```
post_draws(poster, R, par, p)
```

Arguments

`poster`	list output from `fit_cpp` function
`R`	integer number of posterior samples
`par`	if `TRUE` only β and σ^2 are sampled (ω is omitted)
`p`	integer if `par = TRUE`, it specifies the column number of X

Value

list posterior samples

`post_draws_MvT` *Sample R draws from the posterior distributions*

Description

Sample R draws from the posterior distributions

Usage

```
post_draws_MvT(poster, R, par, p)
```

Arguments

`poster`	list output from `fit_cpp` function
`R`	integer number of posterior samples
`par`	if `TRUE` only β and Σ are sampled (ω is omitted)
`p`	integer if `par = TRUE`, it specifies the column number of X

Value

list posterior samples

`pred_bayesMvLMconjugate` *Predictive sampler for Conjugate Bayesian Multivariate Linear Models*

Description

Predictive sampler for Conjugate Bayesian Multivariate Linear Models

Usage

```
pred_bayesMvLMconjugate(X_new, B_samples, Sigma_samples)
```

Arguments

`X_new`	matrix $n_new \times p$ of predictors for new data points
`B_samples`	array of posterior sample for β
`Sigma_samples`	array of posterior samples for Σ

Value

Y_pred matrix of posterior mean for response matrix Y predictions

Y_pred_samples array of posterior predictive sample for response matrix Y

Examples

```
## Generate data
n <- 100
p <- 3
q <- 2
Y <- matrix(rnorm(n*q), nrow = n, ncol = q)
X <- matrix(rnorm(n*p), nrow = n, ncol = p)

## Prior parameters
mu_B <- matrix(0, p, q)
V_B <- diag(10, p)
nu <- 3
Psi <- diag(q)

## Samples from posteriors
n_iter <- 1000
burn_in <- 500
set.seed(1234)
samples <- spBPS::bayesMvLMconjugate(Y, X, mu_B, V_B, nu, Psi, n_iter, burn_in)

## Extract posterior samples
B_samples <- samples$B_samples
Sigma_samples <- samples$Sigma_samples

## Samples from predictive posterior (based posterior samples)
m <- 50
X_new <- matrix(rnorm(m*p), nrow = m, ncol = p)
pred <- spBPS::pred_bayesMvLMconjugate(X_new, B_samples, Sigma_samples)
```

`r_pred_cond` *Draw from the conditional posterior predictive for a set of unobserved covariates*

Description

Draw from the conditional posterior predictive for a set of unobserved covariates

Usage

```
r_pred_cond(data, X_u, d_u, d_us, hyperpar, poster, post)
```

Arguments

`data`	list two elements: first named Y, second named X
`X_u`	matrix unobserved instances covariate matrix
`d_u`	matrix unobserved instances distance matrix
`d_us`	matrix cross-distance between unobserved and observed instances matrix
`hyperpar`	list two elemets: first named δ, second named ϕ
`poster`	list output from `fit_cpp` function
`post`	list output from `post_draws` function

Value

list posterior predictive samples

`r_pred_cond_MvT` *Draw from the conditional posterior predictive for a set of unobserved covariates*

Description

Draw from the conditional posterior predictive for a set of unobserved covariates

Usage

```
r_pred_cond_MvT(data, X_u, d_u, d_us, hyperpar, poster, post)
```

Arguments

`data`	list two elements: first named Y, second named X
`X_u`	matrix unobserved instances covariate matrix
`d_u`	matrix unobserved instances distance matrix
`d_us`	matrix cross-distance between unobserved and observed instances matrix
`hyperpar`	list two elemets: first named α, second named ϕ
`poster`	list output from `fit_cpp_MvT` function
`post`	list output from `post_draws_MvT` function

Value

list posterior predictive samples

`r_pred_joint` *Draw from the joint posterior predictive for a set of unobserved covariates*

Description

Draw from the joint posterior predictive for a set of unobserved covariates

Usage

```
r_pred_joint(data, X_u, d_u, d_us, hyperpar, poster, R)
```

Arguments

`data`	list two elements: first named Y, second named X
`X_u`	matrix unobserved instances covariate matrix
`d_u`	matrix unobserved instances distance matrix
`d_us`	matrix cross-distance between unobserved and observed instances matrix
`hyperpar`	list two elemets: first named δ, second named ϕ
`poster`	list output from `fit_cpp` function
`R`	integer number of posterior predictive samples

Value

list posterior predictive samples

`r_pred_joint_MvT` *Draw from the joint posterior predictive for a set of unobserved covariates*

Description

Draw from the joint posterior predictive for a set of unobserved covariates

Usage

```
r_pred_joint_MvT(data, X_u, d_u, d_us, hyperpar, poster, R)
```

Arguments

`data`	list two elements: first named Y, second named X
`X_u`	matrix unobserved instances covariate matrix
`d_u`	matrix unobserved instances distance matrix
`d_us`	matrix cross-distance between unobserved and observed instances matrix
`hyperpar`	list two elemets: first named α, second named ϕ
`poster`	list output from `fit_cpp` function
`R`	integer number of posterior predictive samples

Value

list posterior predictive samples

`r_pred_marg` *Draw from the marginals posterior predictive for a set of unobserved covariates*

Description

Draw from the marginals posterior predictive for a set of unobserved covariates

Usage

```
r_pred_marg(data, X_u, d_u, d_us, hyperpar, poster, R)
```

Arguments

`data`	list two elements: first named Y, second named X
`X_u`	matrix unobserved instances covariate matrix
`d_u`	matrix unobserved instances distance matrix
`d_us`	matrix cross-distance between unobserved and observed instances matrix
`hyperpar`	list two elemets: first named δ, second named ϕ
`poster`	list output from `fit_cpp` function
`R`	integer number of posterior predictive samples

Value

list posterior predictive samples

r_pred_marg_MvT — *Draw from the joint posterior predictive for a set of unobserved covariates*

Description

Draw from the joint posterior predictive for a set of unobserved covariates

Usage

```
r_pred_marg_MvT(data, X_u, d_u, d_us, hyperpar, poster, R)
```

Arguments

data	list two elements: first named Y, second named X
X_u	matrix unobserved instances covariate matrix
d_u	matrix unobserved instances distance matrix
d_us	matrix cross-distance between unobserved and observed instances matrix
hyperpar	list two elemets: first named α, second named ϕ
poster	list output from fit_cpp function
R	integer number of posterior predictive samples

Value

list posterior predictive samples

sample_index — *Function to sample integers (index)*

Description

Function to sample integers (index)

Usage

```
sample_index(size, length, p)
```

Arguments

size	integer dimension of the set to sample
length	integer number of elements to sample
p	vector sampling probabilities

Value

vector sample of integers

spPredict_BPS — *Perform prediction for BPS accelerated models - loop over prediction set*

Description

Perform prediction for BPS accelerated models - loop over prediction set

Usage

```
spPredict_BPS(data, X_u, priors, coords, crd_u, hyperpar, W, R, J)
```

Arguments

data	list two elements: first named Y, second named X
X_u	matrix unobserved instances covariate matrix
priors	list priors: named μ_b,V_b,a,b
coords	matrix sample coordinates for X and Y
crd_u	matrix unboserved instances coordinates
hyperpar	list two elemets: first named δ, second named ϕ
W	matrix set of stacking weights
R	integer number of desired samples
J	integer number of desired partition of prediction set

Value

list BPS posterior predictive samples

subset_data — *Function to subset data for meta-analysis*

Description

Function to subset data for meta-analysis

Usage

```
subset_data(data, K)
```

Arguments

data	list three elements: first named Y, second named X, third named crd
K	integer number of desired subsets

Value

list subsets of data, and the set of indexes

Examples

```
## Create a list of K random subsets given a list with Y, X, and crd
n <- 100
p <- 3
q <- 2
X <- matrix(rnorm(n*p), nrow = n, ncol = p)
Y <- matrix(rnorm(n*q), nrow = n, ncol = q)
crd <- matrix(runif(n*2), nrow = n, ncol = 2)
subsets <- subset_data(data = list(Y = Y, X = X, crd = crd), K = 10)
```

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